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SUPERCONVERGENT SUM RULE FOR PION PHOTOPRODUCTION ON  $\Lambda^0$

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"Superconvergent" sum rules for certain strong-interaction amplitudes have recently been derived by using the current algebra technique together with the assumption of unsubtracted dispersion relations <sup>1</sup> or on the basis of analyticity and appropriate high-energy behaviour of the amplitude <sup>2</sup>. The Regge-pole model has frequently been invoked in deriving such sum rules <sup>3,4</sup>.

In the present work we study a superconvergent sum rule in the photoproduction of pions on  $\Lambda^0$ . The sum rules obtained for photoproduction of pions on nucleons, discussed recently <sup>4</sup>, are in fair agreement with the experimental data.

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The invariant amplitude in the photoproduction process can be decomposed in terms of four invariant amplitudes <sup>5</sup>, A, B, C, D. They are functions of the two invariants  $\nu = -k \cdot (p_1 + p_2)/2M$  and  $t = -(k - q)^2$  where  $k, q, p_1, p_2$  are the four-momenta of the photon, meson, the initial baryon and the final baryon, respectively. From the Regge-pole theory, we assume that the high-energy behaviour of each amplitude is determined by the leading Regge trajectory which can be exchanged in the t-channel. The recent Regge-pole analysis <sup>6</sup> of high-energy scattering data suggests, if only  $0^-$ ,  $1^-$  and  $2^+$  trajectories are assumed to be important in our case, that the invariant amplitude C behaves like  $\nu^{\alpha(t)-2}$  for large  $\nu$ . Here  $\alpha(t)$  refers to the leading trajectory, the  $\omega$ -trajectory in our case, and for which  $\alpha(0) < 1$  for  $t \sim 0$ . The amplitude C is odd under crossing symmetry, i.e.  $C^*(\nu, t) = -C(-\nu, t)$  and consequently leads to the nontrivial sum rule

$$\int_{-\infty}^{\infty} \text{Im } C(\nu, t) d\nu = 2 \int_0^{\infty} \text{Im } C(\nu, t) d\nu = 0, \quad \text{fixed } t.$$

The pole term contribution to the integral due to the  $\sum$  intermediate state is readily evaluated while the continuum contributions may be approximated using the isobaric model retaining only the  $Y_1^*(1385)$  contribution <sup>7,8</sup>. The crossing symmetry relation implies that we need consider only the direct uncrossed graphs in the s-channel. Assuming that in the contribution coming from  $Y_1^*$  only the  $M_{1+}$  multipole is important ( $E_{1+} \simeq 0$ ), and

making the narrow-width approximation, we obtain the following sum rule for  $t \sim 0$ :

$$g_{NN\pi}(1-\alpha) + 39.4 C_3 \lambda_1 = 0 ,$$

where we have used the  $SU_3$  values for the coupling constant

$$g_{\Sigma\Lambda\pi} = 2/\sqrt{3} (1-\alpha) g_{NN\pi}$$

and the transition magnetic moment  $\mu_{\Sigma\Lambda}$ . The parameter is related to the D/F ratio for the  $\bar{B}BP$  vertex,  $g_{NN\pi}^2/4\pi \sim 15$  and the coupling constants  $C_3$  and  $\lambda_1$  are defined as in ref. <sup>8</sup>.

Calculating  $\lambda_1$  from the experimental width of the decays  $Y_1^{*+} \rightarrow \Lambda \pi^+$  we obtain <sup>9</sup> from the sum rule

$$C_3 = -0.3(1-\alpha) .$$

The constant  $C_3$  can be related <sup>10</sup> to the transition magnetic moment of  $Y_1^* \rightarrow \Lambda \gamma$ . Its calculated value turns out to be  $\sim -\frac{2}{3}\sqrt{2}\mu_p (1.15)$ , where  $\mu_p$  is the total proton magnetic moment and we have used  $\alpha \sim 0.4$ .  $SU_3$  symmetry further leads <sup>11</sup> to a relation between this magnetic moment and the  $N_{3/2}^{*+} \rightarrow p\gamma$  transition magnetic moment. The latter is then predicted to be  $+\frac{2}{3}\sqrt{2}\mu_p (1.30)$ , which compares very well with its experimental value <sup>10</sup>  $+\frac{2}{3}\sqrt{2}\mu_p (1.28 \pm 0.02)$ .

Thus the sum rule derived above is very well satisfied within the framework of  $SU_3$  symmetry and predicts for the transition magnetic moment of  $Y_1^* \Lambda^0 \gamma$  the value  $-\frac{2}{3}\sqrt{2}\mu_p (1.15)$ .

Similar sum rules can also be derived for photoproduction on  $\Sigma$  and  $\Xi$ .

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