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VALENCE ORBITAL IONIZATION POTENTIALS FOR
THIRD-ROW TRANSITION ELEMENTS

by

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ABSTRACT

Valence Orbital Ionization Potentials (VOIPs) for 5d transition elements have been derived by performing fully relativistic self-consistent numerical Local Density atomic calculations. The von Barth-Hedin-Lundqvist local exchange and correlation potential was employed. In order to evaluate the accuracy of the calculated VOIPs, theoretical Ionization Potentials were compared with experimental results obtained from data on the atomic spectra of neutral and of singly, doubly and triply charged 5d transition elements, for the few atomic configurations for which measurements are available. A good agreement was obtained between experimentally derived and theoretical Ionization Potentials, these last calculated by a "transition state" procedure. Comparison was also made with results obtained by performing non-relativistic Local Density calculations. The use of the Kohn-Sham local exchange-only potential was also investigated, in order to assess the effect of correlation corrections included in the von Barth-Hedin-Lundqvist potential. Moment-polarized relativistic Local Density calculations were also performed and compared with the available experimental results.

Key-words: VOIP parameters; Ionization potentials; Third-row transition elements.

1 INTRODUCTION

Semiempirical Molecular Orbital (MO) calculations of the electronic structure of molecules, performed with methods derived from the ZDO (Zero Differential Overlap) approximation, are characterized by the use of atomic spectroscopic information in the determination of the one-center one-electron matrix elements and in the evaluation of two-electron integrals [1-6]. The one-center one-electron integrals (denominated also one-center "core" integrals [1]) are systematically related to Valence Orbital Ionization Potentials (VOIPs) (or VOIPs plus electron affinities) [1], which depend on the charge and configuration of the atom. By definition, a VOIP is the energy difference between the average energy of the states pertaining to a given configuration of the ionized and neutral atom. VOIPs are also required to evaluate the one-center two-electron integrals in Pariser's approximation [7] and the two-electron two-center integrals in the empirical Weiss-Mataga-Nishimoto formula [5,8]. Electron affinities, which are often unknown for transition elements, are also estimated by an isoelectronic extrapolation using the appropriate VOIP parameters [9].

In the semiempirical extended Hückel method, the variation known as the self-consistent charge and configuration (SCCC) method for transition metal complexes [10b] estimates the diagonal Hamiltonian matrix elements as linear combinations of VOIPs for several configurations, where each VOIP is assumed to have a quadratic charge dependency, in order to adequately represent the fractional populations present in the complex.

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For the 3d and 4d transition elements, the dependence of the VOIPs on both charge and configuration can be obtained from the large amount of available data on atomic spectra [11], and thus complete sets of VOIP parameters have been published in the literature [12-14]. For 5d transition elements, however, the situation is quite different, since the experimental data are very scarce and do not allow a reliable estimate of VOIP parameters. Consequently, for third-row transition elements no complete set of VOIPs as a function of the atomic charge and configuration is available in the literature.

For these reasons, we have obtained theoretically a complete set of VOIP parameters, as a function of charge and configuration, for 5d transition elements by performing fully relativistic self-consistent numerical Local Density (LD) atomic calculations [15]. Local Density calculations are an adequate tool to derive VOIPs, since average energies over the states of a configuration are obtained. The von Barth-Hedin-Lundqvist (BHL) local exchange and correlation potential [16,17] was employed and the "transition state" concept [18] was used to define Ionization Potentials.

In Section 2 we give a summary of some uses of VOIPs in semiempirical methods. In Section 3 we describe the theoretical method employed here. In Section 4 we compare theoretical and experimentally derived VOIP, when available. In Section 5 we give calculated VOIP parameters for all 5d elements and in Section 6 we summarize our conclusions.

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2 VOIPs IN SEMIEMPIRICAL METHODS

Most semiempirical MO methods, derived from the ZDO approximation, estimate part or all of the diagonal matrix elements of the one-electron Hamiltonian given by (in Hartrees):

$$H_{\mu\mu}^{AA} = U_{\mu\mu}^{AA} - \sum_{B \neq A} Z_B (\psi_{\mu}^A | R_B^{-1} | \psi_{\mu}^A) \quad (1)$$

where

$$U_{\mu\mu}^{AA} = (\psi_{\mu}^A | -\nabla^2/2 - Z_A R_A^{-1} | \psi_{\mu}^A)$$

from atomic spectroscopic data. In Eq. (1), ψ_{μ}^A is a valence Atomic Orbital (AO) centered on atom A and Z_A is the core (nucleus and inner-shell electrons) charge on atom A. The one-center term $U_{\mu\mu}^{AA}$ is essentially an atomic quantity. The remaining terms in Eq. (1) give the interaction between a valence electron in ψ_{μ}^A with the cores of the other atoms B.

Different semiempirical ZDO methods (CNDO, INDO, NDDO) [1], which attempt to treat explicitly at least the most important electron repulsion integrals, differ mainly in the extent to which the ZDO approximation is invoked in these integrals. The CNDO (Complete Neglect of Differential Overlap) model, for which the ZDO approximation is used for all products of different atomic orbitals $\psi_{\mu} \psi_{\nu}$, relates the one-center one-electron "core"

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integrals $U_{\mu\mu}^{AA}$, Eq. (1), to atomic parameters. In the conventional CNDO/1 parameterization, these integrals are obtained from atomic ionization potentials and Slater-Condon parameters [1]. In the INDO (Intermediate Neglect of Differential Overlap) [1,4] and NDDO (Neglect of Diatomic Differential Overlap) [1] methods, similar treatments are employed, but in these cases the one-center differential overlap integrals are no longer neglected.

An alternative procedure to evaluate the core integrals $U_{\mu\mu}$, adopted in the CNDO/2 and INDO/2 methods, is to use the average between the ionization potential and electron affinity [1]. Unfortunately, electron affinities of transition elements, even for the first transition series, are often unknown. One procedure adopted for transition elements involves determining the electron affinities A_{μ} by an isoelectronic quadratic extrapolation [9] based on ionization potentials and promotion energies, for the appropriate charge and configuration, obtained from atomic spectra.

In the CNDO method, the two-center terms in Eq. (1) have to be approximated in a manner which is consistent with the way the two-electron integrals are treated in the ZDO approximation. Furthermore, the invariance conditions require these terms to be the same for all orbitals ψ_{μ} on atom A. Consequently, the diagonal matrix elements $H_{\mu\mu}^{AA}$ may be written as:

$$H_{\mu\mu}^{AA} = U_{\mu\mu}^{AA} - \sum_{B \neq A} V_{AB} \quad (2)$$

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where V_{AB} represents the interaction of a valence electron in atom A with the core of atom B. In the original CNDO/1 method of Pople and co-workers [1] for an s, p basis set, V_{AB} is calculated using the atom A valence s orbital.

In the CNDO/2 [1] and INDO [1,4,5] methods, the electron-core potential integrals, V_{AB} are not evaluated separately but are related to the electron repulsion integrals:

$$\gamma_{AB} = (\psi_{\mu}^A \psi_{\mu}^A | \psi_{\nu}^B \psi_{\nu}^B) . \quad (3)$$

When focusing on molecular spectroscopy, the usual procedure to determine these integrals empirically [5] is to employ the Weiss-Mataga-Nishimoto formula [8]:

$$\gamma_{AB} \approx \frac{f_{\gamma}}{2f_{\gamma}/(\gamma_{AA} + \gamma_{BB}) + R_{AB}} \quad (4)$$

where R_{AB} is the distance between the two centers in Bohr radii and f_{γ} is a parameter introduced by Weiss [5]. The one-center two-electron integrals are obtained from the Pariser approximation [7]

$$\gamma_{AA} \approx I_A - A_A \quad (5)$$

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where I_A and A_A are the ionization potential and electron affinity, respectively, of an s, p or d electron on atom A, for a given configuration.

The ionization potentials appearing in the semiempirical methods derived from the ZDO approximation may be related to the average of the states of a configuration (VOIP). Furthermore, the possibility of employing VOIPs pertaining to the charge and configuration of the atoms in the molecule would constitute an improvement.

In the semiempirical extended Hückel (EH) method [10a], the Hamiltonian of the system is not explicitly defined, as is the case in methods derived from the ZDO approximation. The diagonal matrix elements of the "effective" Hamiltonian operator are approximated as minus the VOIP of the atom for a given configuration, and the off-diagonal elements are proportional to an average of the diagonal ones weighted by the appropriate orbital overlap. Furthermore, the variation of the EH method, known as the self-consistent charge and configuration (SCCC) method for transition metal complexes [10b], estimates the diagonal Hamiltonian matrix elements as linear combinations of VOIPs for several configurations, where each VOIP is assumed to have a quadratic charge dependency, in order to adequately represent the self-consistent charge and fractional populations present in the complex. This procedure requires extensive tabulations of VOIPs as a function of both charge and configuration.

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3 THEORETICAL METHOD

A. Non-relativistic

The purpose of atomic spin-polarized self-consistent Local Density (LD) calculations [19] based on Density Functional Theory [20] is to solve the set of one-electron equations

$$(h - \epsilon_{1\sigma}) \psi_{1\sigma}(\vec{r}) = 0 \quad (6)$$

where $\psi_{1\sigma}$ is an atomic spin-orbital and the one-electron Hamiltonian is given (in Hartrees) by

$$h = -\nabla^2/2 + V[\rho_{\sigma}(\vec{r})] . \quad (7)$$

The spin density $\rho_{\sigma}(\vec{r})$ at point \vec{r} is defined as a sum over the spin-orbitals $\psi_{1\sigma}(\vec{r})$ with occupation numbers $f_{1\uparrow}$, $f_{1\downarrow}$ for either spin

$$\rho_{\sigma}(\vec{r}) = \sum_{\uparrow} f_{1\sigma} |\psi_{1\sigma}(\vec{r})|^2 . \quad (8)$$

The potential $V[\rho_{\sigma}(\vec{r})]$ is a functional of the spin density ρ_{σ} and includes a Coulomb and an exchange-correlation term. The Coulomb potential V_{COUL} includes both nuclear and electronic contributions

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$$V_{\text{COUL}}[\rho_{\sigma}(\vec{r})] = -\frac{Z}{r} + \int \frac{\rho_{\sigma}(\vec{r}')}{|\vec{r}-\vec{r}'|} d\vec{r}' \quad (9)$$

In the exchange-only LD theory, the local exchange potential $V_x[\rho_{\sigma}(\vec{r})]$ is given by the Kohn-Sham (KS) expression [19]

$$V_x[\rho_{\sigma}(\vec{r})] = -2(3/4\pi)^{1/3} [\rho_{\sigma}(\vec{r})]^{1/3} \quad (10)$$

Improvements were made in the theory, in order to include correlation effects, leading to exchange and correlation local potentials of the general form

$$V_{xc}[\rho_{\sigma}(\vec{r})] = V_x[\rho_{\sigma}(\vec{r})] \left\{ 1 + F(\rho_{\uparrow}, \rho_{\downarrow}) \right\} \quad (11)$$

where the correction factor F is obtained by a fitting procedure to numerical calculations of the correlation energy for a uniform electron gas [16,17].

Non-relativistic LD calculations retain the restriction of spherical symmetry for atoms. Consequently, the spin-orbitals $\psi_{i\sigma}(\vec{r})$ which are solutions of Eq. (6) have the property of being the product of a radial function times a spherical harmonic. In spin-polarized calculations, the

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restriction that the radial functions $R_{nl\sigma}(r)$ have the same values for both spin-up and spin-down electrons is relaxed, leading to different radial functions and, consequently, different spin densities and self-consistent potentials for the two spin orientations.

B. Relativistic

The one-electron Dirac hamiltonian provides the usual starting point for relativistic self-consistent LD calculations and is written (in Hartrees, $c=137.037$) as [15]:

$$h_D = c\tilde{\alpha} \cdot [\vec{p} - (1/c)\vec{A}] + c^2(\tilde{\beta} - 1) + A_0 \quad (12)$$

where $\tilde{\alpha}$ and $\tilde{\beta}$ are the 4x4 Dirac matrices, \vec{p} the momentum operator and (\vec{A}, A_0) a four-component vector potential describing external fields. The one-electron atomic equations are

$$(h_D - \epsilon_{nK}) \psi_{nK\mathbf{m}}(\vec{r}, s) = 0 \quad (13)$$

In the simplest extension of the non-relativistic LD theory, one sets $\vec{A}=0$ and $A_0=V[\rho_\sigma(\vec{r})]$, where $V[\rho_\sigma(\vec{r})]$ includes the Coulomb potential, Eq. (9), and the local exchange-correlation potential, Eqs. (10), (11), as in

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the non-relativistic case. The use of non-relativistic exchange-correlation potentials in relativistic LD calculations is well justified. The effect of relativistic corrections to the non-relativistic local potential (Eq. 10) on the energy levels is negligible for valence shells, becoming significant only for core levels of heavy atoms [21].

The fourth order central field Dirac spinors are

$$\psi_{n\kappa m}(\vec{r}, s) = \begin{bmatrix} r^{-1} P_{n\kappa}(r) \chi_{\kappa m}(\theta, \phi, s) \\ i r^{-1} Q_{n\kappa}(r) \chi_{-\kappa m}(\theta, \phi, s) \end{bmatrix} \quad (14)$$

where $P_{n\kappa}(r)$ and $Q_{n\kappa}(r)$ are respectively the "large" and "small" components. The orbitals $\psi_{n\kappa m}(\vec{r}, s)$ are eigenfunctions of the total angular momentum squared j^2 and of its projection j_z with eigenvalues $j(j+1)$ and m , respectively, and are of given parity. The relativistic quantum number κ is defined by:

$$\kappa = l \quad \text{if } j = l - 1/2 \quad \text{and} \quad \kappa = -(l+1) \quad \text{if } j = l + 1/2 \quad (15)$$

which includes both j and the parity. The two component Pauli spinor $\chi_{\kappa m}$ is a vector-coupled function of a spherical harmonic $Y_l^m(\theta, \phi)$ and a spin function $\xi_\sigma(s)$ [15].

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A set of coupled radial equations is obtained, by substituting the wavefunction of Eq. (14) into the eigenvalue equations (Eqs. (13))[15]

$$c \frac{dQ_{n\kappa}(r)}{dr} - \frac{c\kappa}{r} Q_{n\kappa}(r) + V[\rho(r)]P_{n\kappa}(r) = \epsilon_{n\kappa} P_{n\kappa}(r) \quad (16)$$

$$-c \frac{dP_{n\kappa}(r)}{dr} - \frac{c\kappa}{r} P_{n\kappa}(r) - 2c^2 Q_{n\kappa}(r) + V[\rho(r)]Q_{n\kappa}(r) = \epsilon_{n\kappa} Q_{n\kappa}(r) .$$

These equations can be solved self-consistently, in an analogous way to the non-relativistic equations, since the potential is a functional of the electronic density

$$\rho(r) = \sum_{n\kappa} f_{n\kappa} [P_{n\kappa}^2(r) + Q_{n\kappa}^2(r)] . \quad (17)$$

The moment-polarized scheme, developed by Ellis and Goodman [22], is a relativistic alternative to the spin-polarized non-relativistic theory, since the spin-component s_z is not diagonal in the four-component theory. The moment-polarized approach is based on the twofold Kramers degeneracy, which remains in the Dirac theory [23], and allows different occupancy for \uparrow, \downarrow members of the Kramers doublets and different spatial wavefunctions for each component. In this case, different potentials $V[\rho_\sigma(r)]$ (one for moment up and the other for moment down) are used to determine the \uparrow, \downarrow eigenvalues and eigenvectors, in analogy to the non-relativistic

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spin-polarized case.

The radial equations, for both relativistic and non-relativistic cases, are solved numerically by using a radial mesh of 300 points with a logarithmic distribution, which concentrates a larger number of points near the nucleus.

4 COMPARISON BETWEEN THEORETICAL AND EXPERIMENTALLY DERIVED VOIPs

A. Some details of the calculations

The VOIP for a specific electron of a specific configuration of the neutral atom is defined as [24]:

$$\text{VOIP} = \text{IP} + E'_I - E'_A \quad (18)$$

where IP is the first ionization potential, E'_A the average energy of the given configuration of the neutral atom relative to its ground state, and E'_I the average energy of the corresponding configuration of the ion relative to the ground state of the ionized atom. Similar expressions hold to derive VOIPs for singly and doubly charged atoms.

As mentioned in the introduction, in a LD calculation the VOIP is given by

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$$\text{VOIP} = E_I - E_A \quad (19)$$

where E_A and E_I are the average energies over the states of a given configuration of the neutral and ionized atom, respectively, obtained directly from the LD calculations. Both definitions (Eqs. (18) and (19)), of course, represent the same quantity.

Since the potential $V[\rho(r)]$ in the LD theory depends only on the electronic density, it is the same for all states within a configuration. Therefore, there is no need for averaging over the "LS configuration" (in the non-relativistic case) or over a "jj configuration" (in the relativistic case), as in the Hartree-Fock-Dirac method. On the other hand, considering a single "jj configuration" (in the relativistic LD or Dirac-Fock methods) is meaningful only when "jj-coupling" dominates. Furthermore, the use of pure "jj configurations" may be misleading when a comparison is made with non-relativistic results obtained in LS-coupling. The appropriate procedure, when dealing with open-shell systems in intermediate coupling, would therefore be to average over all the "jj configurations" associated to a single LS one [15,25]. In this case, the electronic density $\rho(r)$ (Eq. (17)) has to be replaced by the average [15]

$$\langle \rho(r) \rangle = \sum_{n\kappa} \langle f_{n\kappa} \rangle [P_{n\kappa}^2(r) + Q_{n\kappa}^2(r)] \quad (20)$$

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where $\langle f_{n\kappa} \rangle$ is the average occupation number

$$\langle f_{n\kappa} \rangle \equiv \langle f_{nlj} \rangle = (f_{nl}^0 / f_{nl}^0) f_{nlj}^0 . \quad (21)$$

Here, f_{nl} is the occupation number of the "nl" main shell; f_{nl}^0 and f_{nlj}^0 are the degeneracies of the "nl" main shell and the "nlj" subshell, respectively.

The procedure described above, based on the average occupation numbers $\langle f_{n\kappa} \rangle$, was employed to derive VOIPs in the relativistic calculations reported here, since most of the available atomic experimental data have been assigned LS-designations or are listed with miscellaneous designations owing to the departure from LS-coupling [11]. The atomic spectra is analysed within jj-coupling only for elements in the vicinity of gold. Furthermore, most semiempirical MO methods are parameterized using non-relativistic basis sets.

No account was taken of the Breit interaction term or higher-order relativistic corrections, and corrections for the finite size of the nucleus were omitted. The effect of these corrections on the VOIPs for valence shells is negligible [26].

Derivations of VOIPs would require two calculations, one to obtain the energy of the neutral atom and the other for the ionized atom. However,

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with the use of the "transition state concept", only one calculation needs to be performed to obtain each VOIP. In fact, it has been demonstrated that, up to second order, the energy needed to ionize an electron from one orbital is equal to the absolute value of the orbital energy in a self-consistent calculation with 1/2 electron removed from the orbital [18]. This procedure not only reduces the computations by 50%, but also assures that in many cases better accuracy is achieved, since it avoids numerical errors due to small differences between very large numbers.

B. Comparison with experimental results

Theoretical VOIPs for several charges and configurations of 5d transition elements are given in Tables I-III. Non-relativistic (NR) non-spin-polarized (NP) LD calculations employing the Kohn-Sham (KS) local exchange-only potential are designated (NR-KS-NP). Fully relativistic (R) non-moment-polarized (NP) LD calculations were also performed employing both the Kohn-Sham (KS) local exchange-only potential (R-KS-NP) and the von Barth-Hedin-Lundqvist (BHL) local exchange and correlation potential (R-BHL-NP). The fully relativistic (R) LD calculations, employing the von Barth-Hedin-Lundqvist (BHL) local exchange and correlation potential and the moment-polarized (P) scheme developed by Ellis and Goodman [22], were designated (R-BHL-P). The experimental values presented in Tables I-III were obtained from data on the atomic spectra of neutral and of singly, doubly and triply charged 5d transition elements, for the few atomic configurations for which measurements are reported [11,27-51]. Only configurations for which at least 90% of the states are known were

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considered, unless otherwise specified.

As is well known, the relativistic treatment gives VOIPs which are larger for the s and p electrons (the orbitals are contracted) and smaller for the d electrons (the orbitals are expanded), as compared to non-relativistic calculations. These relativistic effects can be observed comparing the (NR-KS-NP) and the (R-KS-NP) results in Tables I-III. The lower energies (and the larger VOIPs) for the 6s and $6p_{1/2}$ orbitals, obtained in the relativistic calculations, are consistent with their penetration into the core region. The relativistic treatment allows the description of the contraction of these orbitals, which is a consequence of the proximity of the nucleus. For the orbitals that extend outside the core region, as the 5d orbitals, the core contraction yields a greater screening of the nucleus, and so the electrons experience a weaker potential. This indirect relativistic effect results in the higher energies, and smaller VOIPs, for the 5d orbitals.

In comparing the results of the (NR-KS-NP) and (R-KS-NP) calculations, as shown in Tables I-III, with the experimental values, it may be seen that the relativistic 6s and 6p calculated VOIPs are always in better agreement with the measured values, as compared to the non-relativistic. The same is not true for the 5d VOIPs, for which the non-relativistic values compare better with experiment. This is possibly due to a compensation of errors between the use of the KS potential (no correlation) and the

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non-relativistic treatment.

The von Barth-Hedin-Lundqvist exchange and correlation local potential yields VOIPs that are systematically $\sim 1\text{eV}$ higher than the values obtained using the simple exchange-only Kohn-Sham potential. The rather large effect due to correlation corrections can be observed comparing the (R-KS-NP) and the (R-BHL-NP) results for the 5d, 6s and 6p electrons in Tables I-III. Comparing with experimental values, it may be observed that consideration of correlation effects improves the VOIPs of 5d and 6p electrons in the vast majority of cases. For the 6s electrons no improvement may be observed on the average.

In general, a good agreement was obtained between experimentally derived and relativistic non-polarized theoretical VOIPs, these last obtained using the von Barth-Hedin-Lundqvist exchange and correlation local potential (R-BHL-NP), for almost all atomic configurations for which measurements are available. On the other hand, some discrepancies should be pointed out, mainly for the $5d^n(d)$ and $5d^{n-1}6s(s)$ configurations of the neutral 5d transition elements. The discrepancies noticed are invariably an overbinding found in the calculated VOIPs, as compared to experiment. This overbinding is stronger for the $5d^n(d)$ configuration. It has been shown [52,53] for the 3d series that the local potential produces systematic overbinding in calculated ionization potentials. Our calculations indicate that the same is true for the 5d series, at least for the atoms considered here, for which experimental data was available.

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Attempting to improve even further the VOIP values, we have performed relativistic moment-polarized calculations with the BHL exchange-correlation potential (R-BHL-P). Moment-polarized calculations usually improve the VOIP value when the ionized electron is a minority spin 5d electron, although the overbinding is somewhat overcorrected for some atomic configurations. The VOIP value is also improved when the ionized electron is a minority spin 6s electron, but only for atoms or ions that have minority spin 5d electron. For atoms at the beginning of the 5d series, the overbinding is overcorrected. Consequently, no systematic improvement has been obtained by performing moment-polarized calculations. For this reason, we chose the moment-restricted relativistic LD method with the von Barth-Hedin-Lundqvist potential (R-BHL-NP) to derive the complete set of VOIPs for 5d transition elements. The VOIPs calculated in this manner compare better with experiment on the average, for the cases in which comparison with measured data is possible. Most calculated VOIPs are within 0.5 eV of the experimental value; results are in general better for the charged atoms.

5 VOIPs FOR 5d TRANSITION ELEMENTS

The calculated VOIPs were represented by a quadratic polynomial form

$$\text{VOIP}(q) = C_2 q^2 + C_1 q + C_0 \quad (22)$$

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where q is the net atomic charge. The values of the coefficients C_0 , C_1 and C_2 , for the VOIPs of $5d_{5/2}$, $5d_{3/2}$, $6s_{1/2}$, $6p_{3/2}$ and $6p_{1/2}$ orbitals for several configurations, are compiled in Tables IV A and B. These coefficients were obtained by fitting the calculated values for the charges $q=0$, $+1$ and $+2$. The VOIP curves coefficients for the j -weighted average of the $j=\pm 1/2$ VOIPs are also tabulated in Tables IV A and B.

An attempt to estimate VOIPs from experimental data for 5d transition elements was made by Jostes [54], for neutral atoms only. The small amount of available data on atomic spectra did not allow the determination of the charge dependence of the VOIPs. Moreover, even for neutral atoms, the experimental data were not enough to allow the calculation of the average energies of the configurations and some assumptions had to be made in order to estimate the VOIPs.

Relativistic theoretical VOIPs have been employed in semiempirical calculations of molecules containing lanthanides [55,56] and actinides [57]; however, only values for neutral atoms in the ground state configuration were considered.

The present parameter set should prove useful for semiempirical MO calculations, since this is the only complete set of VOIPs derived for all 5d transition elements, as a function of both charge and configuration. Consideration of the dependence of VOIPs on charge and configuration, when parametrizing semiempirical methods, should improve the results of molecular

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calculations. The comparison that we have made with experimental values has proved that the present theoretical method is capable of providing accurate values. It should be observed that, in most cases, the comparisons made involve atoms at the beginning and end of the 5d transition series. This is due to the increased complexity (and thus difficult interpretation) of the experimental spectra of the atoms in the middle of the series. For these intermediate atoms our calculated values should prove most useful. Furthermore, the present work also provides a parameter set which can be used in "fully relativistic" semiempirical MO calculations, i.e. calculations where a jj-basis set is required [58].

6 CONCLUSIONS

A complete set of VOIPs for 5d transition elements have been derived by performing fully relativistic self-consistent numerical Local Density atomic calculations. A good agreement was obtained between theoretical and experimentally derived VOIPs, for the atomic configurations for which measurements are available. The present parameter set should prove useful in semiempirical Molecular Orbital calculations for molecules containing 5d transition elements, in both relativistic and non-relativistic frameworks.

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TABLE CAPTIONS

Table I.A - VOIPs for neutral 5d atoms^(a).

- (a) In units of eV.
- (b) The type of electron being ionized (in parenthesis) and the configuration.
- (c) Non-relativistic (NR) non-spin-polarized (NP) calculations employing the Kohn-Sham (KS) potential.
- (d) Relativistic (R) non-moment-polarized (NP) calculations employing the Kohn-Sham (KS) potential.
- (e) Relativistic (R) non-moment-polarized (NP) calculations employing the von Barth-Hedin-Lundqvist (BHL) potential.
- (f) Relativistic (R) moment-polarized (P) calculations employing the von Barth-Hedin-Lundqvist (BHL) potential.
- (g) The j-weighted average of the $j=\ell\pm 1/2$ VOIPs are tabulated in order to compare with those obtained non-relativistically and with the experimental values.
- (h) Experimental values from data in references (11), (27)-(51).

Table I.B - VOIPs for neutral 5d atoms (continued)^(a).

- (a) In units of eV.
- (b)-(h) See footnotes in Table I.A.

Table II.A - VOIPs for singly charged 5d atoms^(a).

- (a) In units of eV.

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(b)-(h) See footnotes in Table I.A.

Table II.B - VOIPs for singly charged 5d atoms (continued)^(a).

(a) In units of eV.

(b)-(h) See footnotes in Table I.A.

(i) 80% of states known.

Table III - VOIPs for doubly charged 5d atoms^(a).

(a) In units of eV.

(b)-(h) See footnotes in Table I.A.

Table IV.A - Parameters for VOIP curves as a function of the charge q

$$(\text{VOIP} = C_2 q^2 + C_1 q + C_0)^{(a)}$$

(a) In units of eV.

(b) n corresponds to the configuration of the neutral atom.

(c) V.O. stands for valence orbital from which electron is ionized. Fraction in parenthesis is j quantum number. No parenthesis designates j -weighted average.

Table IV.B - Parameters for VOIP curves as a function of the charge q

$$(\text{VOIP} = C_2 q^2 + C_1 q + C_0) \text{ (continued)}^{(a)}$$

(a) In units of eV.

(b) n corresponds to the configuration of the neutral atom.

(c) V.O. stands for valence orbital from which electron is ionized. Fraction in parenthesis is j quantum number. No parenthesis designates j -weighted average.

Configuration ^(b)	n	NR-KS-NP ^(c)	J	R-KS-NP ^(d)	R-BHL-NP ^(e)	R-BHL-P ^(f)	Experimental ^(h)
5d ⁿ (d)							
Ir	9	7.7	5/2	7.0 > 7.4 ^(g)	8.3 > 8.7 ^(g)	7.8 > 8.3 ^(g)	7.0
Pt	10	8.5	3/2	8.1 > 8.2	9.5 > 9.5	9.0 > 9.4	8.6
5d ⁿ⁻¹ 6s(d)							
Hf	4	5.1	5/2	4.3 > 4.5	5.4 > 5.6	6.1 > 6.3	5.3
Pt	10	11.2	3/2	4.8 > 10.1	10.9 > 11.5	10.2 > 10.8	10.8
Au	11	12.2	5/2	9.5 > 11.0	12.3 > 12.4	11.7 > 12.1	11.9
5d ⁿ⁻² 6s ² (d)							
Hf	4	6.7	3/2	10.3 > 5.5	6.5 > 6.7	6.9 > 7.1	6.5
Ta	5	8.0	5/2	5.8 > 6.7	7.1 > 7.9	7.4 > 8.5	7.5
Au	11	15.3	3/2	6.4 > 13.2	8.3 > 14.7	8.9 > 14.2	14.3
Hg	12	16.6	5/2	12.5 > 14.3	15.7 > 15.8	13.5 > 15.6	15.6
5d ⁿ⁻¹ 6p(d)							
Au	11	13.7	3/2	13.5 > 12.8	17.0 > 14.2	14.8 > 13.9	13.7

TABLE I.A

Configuration ^(b)	n	NR-KS-NP ^(c)	J	R-KS-NP ^(d)	R-BHL-NP ^(e)	R-BHL-P ^(f)	Experimental ^(h)
$5d^{n-1}6s(s)$	4	5.6	1/2	6.8	7.7	8.4	7.4
	Hf						8.4
	Ir	6.4	1/2	8.2	9.4	9.8	8.4
	Pt	6.5	1/2	8.5	9.6	9.9	8.8
$5d^{n-2}6s^2(s)$	11	6.6	1/2	8.7	9.9	10.0	9.2
	Au						9.2
	4	6.3	1/2	7.2	8.3	7.4	7.8
	Hf						7.8
$5d^{n-2}6s6p(s)$	5	6.7	1/2	7.7	8.8	7.7	8.5
	Ta						8.5
	10	7.7	1/2	9.4	10.6	10.0	9.8
	Pt						9.8
	11	7.8	1/2	9.6	10.8	10.5	10.1
	Au						10.1
$5d^{n-1}6p(p)$	12	7.9	1/2	9.9	11.1	10.9	10.4
	Hg						10.4
	11	8.7	1/2	10.9	12.1	12.6	12.1
	Au						12.1
$5d^{n-2}6s6p(p)$	12	8.9	1/2	11.3	12.4	12.8	12.0
	Hg						12.0
	11	3.2	3/2	3.4	4.3	4.5	4.3
	Au						4.3
			1/2	4.0	4.9	5.1	
				3.6 ^(g)	4.5 ^(g)	4.7 ^(g)	
$5d^{n-2}6s6p(p)$	11	3.9	3/2	3.8	4.7	5.1	5.4
	Au						5.4
			1/2	4.5	5.5	6.0	
				4.0	5.0	5.4	
Hg	12	3.9	3/2	3.8	4.7	5.1	4.9
			1/2	4.6	5.6	6.0	

TABLE I.B

Configuration ^(b)	n	NR-KS-NP ^(c)	J	R-KS-NP ^(d)	R-BHL-NP ^(e)	R-BHL-NP ^(f)	Experimental ^(h)
5d ⁿ (d)							
Hf	3	11.6	5/2	11.0 > 11.2 ^(g)	12.2 > 12.5 ^(g)	12.9 > 13.1 ^(g)	12.2
Au	10	20.6	3/2	11.6 > 19.3 > 20.0	12.8 > 20.9 > 22.6	13.5 > 20.7 > 22.4	21.1
5d ⁿ⁻¹ 6s(d)							
Hf	3	13.7	5/2	12.5 > 12.7	13.8 > 14.0	14.4 > 14.7	14.3
Au	10	23.9	3/2	13.1 > 21.7 > 22.5	23.3 > 24.0	22.6 > 23.3	23.8
Hg	11	25.4	3/2	23.5 > 23.8	25.1 > 25.4	24.4 > 25.1	25.0
5d ⁿ⁻² 6s ² (d)							
Hf	3	15.9	5/2	14.1 > 14.4	15.5 > 15.8	15.7 > 15.9	16.1
Hg	11	29.0	3/2	14.7 > 25.7 > 26.5	16.1 > 27.3 > 28.1	16.3 > 26.8 > 27.6	28.1
5d ⁿ⁻¹ 6p(d)							
Hf	3	14.6	5/2	13.6 > 13.8	14.9 > 15.2	15.5 > 15.7	15.0
Au	10	25.1	3/2	14.2 > 23.3 > 24.0	15.6 > 24.8 > 25.6	16.1 > 24.2 > 24.9	25.4
Hg	11	26.6	3/2	23.3 > 24.6 > 25.4	26.7 > 26.2 > 27.0	26.0 > 25.9 > 26.7	26.6

TABLE II.A

Configuration ^(b)	n	NR-KS-NP ^(c)	J	R-KS-NP ^(d)	R-BHL-NP ^(e)	R-BHL-p ^(f)	Experimental ^(h)
$Sd^{n-1}6s(s)$	3	12.1	1/2	13.5	14.6	15.3	14.3
	10	15.0	1/2	17.7	19.0	19.3	18.5
	11	15.3	1/2	18.2	19.5	19.7	18.8
$5d^{n-2}6s^2(s)$	3	13.3	1/2	14.4	15.6	15.0	15.7
	10	16.4	1/2	18.9	20.2	19.6	19.6
	11	16.7	1/2	19.4	20.7	20.4	19.9
$5d^{n-2}6s6p(s)$	3	13.9	1/2	15.2	16.4	17.1	16.7 ⁽ⁱ⁾
	11	17.5	1/2	20.5	21.9	22.5	21.8
	3	8.6	3/2	8.7 > 8.9 ^(g)	9.6 > 9.8 ^(g)	10.1 > 10.4 ^(g)	9.5
$5d^{n-1}6p(p)$	10	10.2	3/2	10.4 > 10.8	11.4 > 11.9	11.8 > 12.2	11.7
	11	10.3	1/2	11.6 > 11.0	12.7 > 12.0	13.0 > 12.3	11.6
	3	9.4	3/2	10.6 > 11.0	11.6 > 12.0	11.9 > 12.3	11.6
$5d^{n-2}6s6p(p)$	3	9.4	3/2	9.3 > 9.5	10.2 > 10.5	10.8 > 11.1	11.2
	11	11.3	1/2	11.2 > 11.7	12.3 > 12.8	12.9 > 13.4	13.1 ⁽ⁱ⁾
	11	11.3	1/2	12.7 > 11.7	13.8 > 12.8	14.4 > 13.4	13.1 ⁽ⁱ⁾

TABLE II.B

Configuration (b)	n	NR-KS-NP (c)	J	R-KS-NP (d)	R-BHL-NP (e)	R-BHL-P (f)	Experimental (h)
$5d^n$ (d)							
Hf	2	21.4	5/2	20.4 > 20.7 (g)	21.8 > 22.1 (g)	22.4 > 22.6 (g)	22.6
Hg	10	35.1	3/2	21.1	22.5	23.1	
			5/2	33.4 > 34.2	35.0 > 35.8	34.9 > 35.7	34.9
			3/2	35.4	37.1	36.9	
$5d^{n-1}6s$ (d)							
Hf	2	23.9	5/2	22.5 > 22.7	23.9 > 24.2	24.4 > 24.6	24.5
			3/2	23.1	24.6	25.0	
$5d^{n-1}6p$ (d)							
Hf	2	24.8	5/2	23.6 > 23.8	25.0 > 25.3	25.4 > 25.6	25.8
			3/2	24.2	25.7	26.0	
$5d^{n-1}6s$ (s)							
Hf	2	19.9	1/2	21.5	22.7	23.2	22.5
Hg	10	25.0	1/2	28.6	29.9	30.3	28.6
$5d^{n-2}6s^2$ (s)							
Hf	2	21.3	1/2	22.8	24.0	23.7	24.1
$5d^{n-2}6s6p$ (s)							
Hf	2	21.9	1/2	23.5	24.8	25.3	24.7
$5d^{n-1}6p$ (p)							
Hf	2	15.4	3/2	15.5 > 15.8	16.5 > 16.8	16.9 > 17.3	17.0
Hg	10	18.8	1/2	16.4	17.5	18.0	
			3/2	19.1 > 19.7	20.2 > 20.9	20.6 > 21.3	19.9
			1/2	21.0	22.2	22.6	
$5d^{n-2}6s6p$ (p)							
Hf	2	16.5	3/2	16.4 > 16.7	17.4 > 17.8	18.0 > 18.4	17.9
			1/2	17.4	18.5	19.1	

TABLE III

	Configu- ration (b)	V.O. (a)	Hf n=4	Ta n=5	W n=6	Re n=7	Os n=8	Ir n=9	Pt n=10	Au n=11	Hg n=12
C ₂	d ⁿ	d(5/2)	0.980	0.860	0.780	0.800	0.815	0.775	0.740		
C ₂	d ⁿ	d(3/2)	0.965	0.855	0.840	0.780	0.725	0.775	0.750		
C ₂	d ⁿ	d	0.925	0.830	0.825	0.770	0.770	0.815	0.715		
C ₂	d ⁿ⁻¹ s	d(5/2)	0.845	0.825	0.740	0.745	0.695	0.690	0.700	0.700	
C ₂	d ⁿ⁻¹ s	d(3/2)	0.855	0.795	0.730	0.710	0.690	0.725	0.700	0.700	
C ₂	d ⁿ⁻¹ s	d	0.900	0.855	0.695	0.780	0.665	0.650	0.750	0.700	
C ₂	d ⁿ⁻¹ p	d(5/2)	0.855	0.820	0.730	0.730	0.725	0.715	0.700	0.750	
C ₂	d ⁿ⁻¹ p	d(3/2)	0.775	0.805	0.780	0.705	0.780	0.760	0.700	0.800	
C ₂	d ⁿ⁻¹ p	d	0.815	0.855	0.690	0.770	0.750	0.650	0.750	0.700	
C ₂	d ⁿ⁻² s ²	d(5/2)		0.715	0.715	0.650	0.650	0.650	0.650	0.600	0.600
C ₂	d ⁿ⁻² s ²	d(3/2)		0.670	0.640	0.700	0.600	0.600	0.700	0.600	0.650
C ₂	d ⁿ⁻² s ²	d		0.705	0.685	0.700	0.650	0.600	0.650	0.550	0.650
C ₁	d ⁿ	d(5/2)	6.660	7.420	8.060	8.500	8.955	9.475	9.980		
C ₁	d ⁿ	d(3/2)	6.805	7.535	8.080	8.660	9.225	9.575	10.050		
C ₁	d ⁿ	d	6.825	7.510	8.025	8.590	9.090	9.455	10.055		
C ₁	d ⁿ⁻¹ s	d(5/2)	7.565	8.025	8.680	9.065	9.615	10.030	10.400	10.800	
C ₁	d ⁿ⁻¹ s	d(3/2)	7.635	8.215	8.810	9.270	9.730	10.125	10.600	11.000	
C ₁	d ⁿ⁻¹ s	d	7.500	8.035	8.815	9.060	9.705	10.150	10.350	10.900	
C ₁	d ⁿ⁻¹ p	d(5/2)	7.535	8.040	8.610	9.010	9.425	9.855	10.300	10.550	
C ₁	d ⁿ⁻¹ p	d(3/2)	7.775	8.185	8.660	9.185	9.460	9.920	10.400	10.600	
C ₁	d ⁿ⁻¹ p	d	7.655	8.035	8.730	8.990	9.450	10.050	10.250	10.700	
C ₁	d ⁿ⁻² s ²	d(5/2)		8.755	9.155	9.650	10.050	10.450	10.850	11.300	11.700
C ₁	d ⁿ⁻² s ²	d(3/2)		8.890	9.380	9.700	10.300	10.700	10.900	11.500	11.750
C ₁	d ⁿ⁻² s ²	d		8.785	9.245	9.600	10.150	10.600	10.950	11.450	11.650
C ₀	d ⁿ	d(5/2)	4.560	5.320	6.060	6.800	7.530	8.250	8.980		
C ₀	d ⁿ	d(3/2)	5.030	5.910	6.780	7.660	8.550	9.450	10.400		
C ₀	d ⁿ	d	4.750	5.560	6.350	7.140	7.940	8.730	9.530		
C ₀	d ⁿ⁻¹ s	d(5/2)	5.390	6.350	7.280	8.190	9.090	9.980	10.900	11.800	
C ₀	d ⁿ⁻¹ s	d(3/2)	5.910	6.990	8.060	9.120	10.180	11.250	12.300	13.400	
C ₀	d ⁿ⁻¹ s	d	5.600	6.610	7.590	8.560	9.530	10.500	11.500	12.400	
C ₀	d ⁿ⁻¹ p	d(5/2)	6.510	7.540	8.560	9.560	10.550	11.530	12.500	13.500	
C ₀	d ⁿ⁻¹ p	d(3/2)	7.050	8.210	9.360	10.510	11.660	12.820	14.000	15.200	
C ₀	d ⁿ⁻¹ p	d	6.730	7.810	8.880	9.940	11.000	12.000	13.100	14.200	
C ₀	d ⁿ⁻² s ²	d(5/2)		7.630	8.730	9.800	10.900	11.900	12.900	14.000	15.000
C ₀	d ⁿ⁻² s ²	d(3/2)		8.340	9.580	10.800	12.000	13.200	14.500	15.700	17.000
C ₀	d ⁿ⁻² s ²	d		7.910	9.070	10.200	11.300	12.400	13.500	14.700	15.800

TABLE IV.A

	Configu- ration ^(b)	V.O. ^(c)	Hf n=4	Ta n=5	W n=6	Re n=7	Os n=8	Ir n=9	Pt n=10	Au n=11	Hg n=12
C ₂	d ⁿ⁻¹ s	s(1/2)	0.600	0.570	0.550	0.510	0.505	0.535	0.460	0.475	
C ₂	d ⁿ⁻² s ²	s(1/2)	0.525	0.530	0.545	0.540	0.465	0.450	0.600	0.500	0.550
C ₂	d ⁿ⁻² sp	s(1/2)	0.560	0.585	0.550	0.550	0.550	0.500	0.500	0.550	0.500
C ₂	d ⁿ⁻¹ p	p(3/2)	0.615	0.585	0.615	0.590	0.655	0.570	0.575	0.680	
C ₂	d ⁿ⁻¹ p	p(1/2)	0.620	0.550	0.560	0.655	0.540	0.570	0.645	0.615	
C ₂	d ⁿ⁻¹ p	p	0.600	0.550	0.595	0.630	0.600	0.520	0.580	0.590	
C ₂	d ⁿ⁻² p ²	p(3/2)	0.585	0.565	0.525	0.525	0.615	0.600	0.630	0.655	0.675
C ₂	d ⁿ⁻² p ²	p(1/2)	0.580	0.605	0.560	0.605	0.585	0.560	0.630	0.595	0.605
C ₂	d ⁿ⁻² p ²	p	0.600	0.545	0.520	0.585	0.590	0.635	0.580	0.670	0.600
C ₂	d ⁿ⁻² sp	p(3/2)	0.610	0.580	0.530	0.520	0.600	0.620	0.535	0.650	0.660
C ₂	d ⁿ⁻² sp	p(1/2)	0.585	0.590	0.615	0.580	0.535	0.580	0.570	0.555	0.635
C ₂	d ⁿ⁻² sp	p	0.585	0.565	0.575	0.575	0.560	0.640	0.565	0.635	0.650
C ₁	d ⁿ⁻¹ s	s(1/2)	6.300	6.690	7.050	7.470	7.785	7.995	8.420	8.675	
C ₁	d ⁿ⁻² s ²	s(1/2)	6.825	7.110	7.365	7.680	8.105	8.450	8.400	8.900	9.050
C ₁	d ⁿ⁻² sp	s(1/2)	6.720	6.945	7.250	7.550	7.850	8.200	8.500	8.650	9.000
C ₁	d ⁿ⁻¹ p	p(3/2)	5.045	5.355	5.555	5.830	5.935	6.290	6.475	6.460	
C ₁	d ⁿ⁻¹ p	p(1/2)	5.340	5.750	6.020	6.135	6.580	6.790	6.865	7.155	
C ₁	d ⁿ⁻¹ p	p	5.160	5.550	5.715	5.910	6.200	6.540	6.660	6.830	
C ₁	d ⁿ⁻² p ²	p(3/2)	5.445	5.705	6.025	6.225	6.255	6.500	6.610	6.735	6.875
C ₁	d ⁿ⁻² p ²	p(1/2)	5.760	5.985	6.320	6.485	6.745	7.020	7.110	7.415	7.585
C ₁	d ⁿ⁻² p ²	p	5.500	5.865	6.140	6.245	6.430	6.595	6.860	6.890	7.200
C ₁	d ⁿ⁻² sp	p(3/2)	5.370	5.660	6.010	6.240	6.300	6.440	6.795	6.750	6.920
C ₁	d ⁿ⁻² sp	p(1/2)	5.745	6.030	6.255	6.560	6.895	7.060	7.290	7.535	7.595
C ₁	d ⁿ⁻² sp	p	5.545	5.805	6.075	6.275	6.520	6.580	6.905	6.995	7.150
C ₀	d ⁿ⁻¹ s	s(1/2)	7.700	8.140	8.500	8.820	9.110	9.370	9.620	9.850	
C ₀	d ⁿ⁻² s ²	s(1/2)	8.250	8.760	9.190	9.580	9.930	10.200	10.600	10.800	11.100
C ₀	d ⁿ⁻² sp	s(1/2)	9.120	9.670	10.200	10.600	11.000	11.400	11.700	12.100	12.400
C ₀	d ⁿ⁻¹ p	p(3/2)	3.950	4.050	4.130	4.180	4.210	4.240	4.250	4.260	
C ₀	d ⁿ⁻¹ p	p(1/2)	4.340	4.500	4.620	4.710	4.780	4.840	4.890	4.930	
C ₀	d ⁿ⁻¹ p	p	4.080	4.200	4.290	4.360	4.400	4.440	4.460	4.480	
C ₀	d ⁿ⁻² p ²	p(3/2)	4.770	4.930	5.050	5.150	5.230	5.300	5.360	5.410	5.450
C ₀	d ⁿ⁻² p ²	p(1/2)	5.460	5.710	5.920	6.110	6.270	6.420	6.560	6.690	6.810
C ₀	d ⁿ⁻² p ²	p	5.000	5.190	5.340	5.470	5.580	5.670	5.760	5.840	5.900
C ₀	d ⁿ⁻² sp	p(3/2)	4.220	4.360	4.460	4.540	4.600	4.640	4.670	4.700	4.720
C ₀	d ⁿ⁻² sp	p(1/2)	4.670	4.880	5.030	5.160	5.270	5.360	5.440	5.510	5.570
C ₀	d ⁿ⁻² sp	p	4.370	4.530	4.650	4.750	4.820	4.880	4.930	4.970	5.000

TABLE IV. B

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