# The Three-Center, $\chi$-Electron Chemical Bond 

Myriam S. de Giambiagi, Mario Giambiagi and Jorge Herrera* Centro Brasileiro de Pesquisas Físicas<br>Rua Dr. Xavier Sigaud, 150<br>22290-180 - Rio de Janeiro - RJ, Brasil<br>*Centro Latino Americano de Física,<br>Av. Wenceslau Braz 71, fundos,<br>22290 - Rio de Janeiro, RJ - Brasil


#### Abstract

A definition is proposed for the number of electrons $\chi$ involved in a three-center bond, based upon the corresponding two-center bond indices. It is seen that the sign of the three-center index does not depend on $\chi$. The number of electrons is fractionary, ranging from about 1 to somewhat more than 4 in the systems considered here.


Key-words: Three-center bond.

## 1 Introduction

The concept of three-center bond is almost contemporary of the Lewis two-center electron pair bond [1]. A distinction is made between two-electron (2e) and four-electron (4e) threecenter (3c) bonds. $H_{3}^{+}$or diborane are taken as paradigms of 3 c -2e bonds and $(F H F)^{-}$ of $3 \mathrm{c}-4 \mathrm{e}$ bonds [1].

We have introduced a three-center bond index [2] in satisfactory agreement with certain experimental data. The values obtained have negative sign. Sannigrahi and Kar [3] affirm that 3 c bond indices have no chemical significance unless they are positive. In Ref. [4], it is asserted that negative values could be associated to (3c-2e) bonds, while positive values should indicate ( $3 \mathrm{c}-4 \mathrm{e}$ ) bonds. We show elsewhere that the sign has a straightforward meaning [5] and here that in MO theory the number of electrons taking part in such a bond may be seen from a different viewpoint.

Actually, the Lewis model of two electrons in a bond is inconsistent with most of the MO indices associated with a chemical bond. The original Coulson bond order [6] has been devised for the $\pi$ electrons of alternant hydrocarbons; $\pi$ systems including heteroatoms led to bond orders which are not comparable with C-C bond orders [7]. Anyway, almost universal consent assigns for example a bond order of 2 for the $\mathrm{C}=\mathrm{C}$ bond in ethylene [8], while under the Lewis octet viewpoint there would be four electrons in this bond. Very few examples may be found in early literature which throw $\pi$ population wholly on the bonds [9, 10]. More recently, a theory considering fluctuations in orbital domains [11, 12] describes these domains along a classical bond with population close to 2 with a small fluctuation from this value. The overwhelming majority of population analysis, of which Mulliken's [13] is by far the most popular, assigns a bond value of 1,2 and 3 for single, double and triple bonds respectively.

When all-valence-electrons calculations were introduced, Hoffmann's EHT (extended Huckel theory) [14] used Mulliken's population analysis. The other approximation dealing with all-valence-electrons at that time was CNDO (complete neglect of differential overlap) with its alternative INDO (incomplete neglect of differential overlap) and, in particular, the CNDO/2 variation [15]. Mulliken's orbital-orbital population lends itself to be contracted to an atom-atom population; CNDO orbital-orbital population does not. In order to compare EH and CNDO/2 results, Wiberg [16] was obliged to devise a new bond index for CNDO, by the way in a very humble footnote. Trindle [17] proposed for
it a subdivision into self-charge and active charge analogous to Mulliken's atomic and overlap populations. MINDO/3 [18] and MNDO [19] came later.

A few years after the work of Wiberg, which did not receive the full deserved attention, we proposed a bond index which generalized Wiberg's when non-orthogonal bases were used. Although we used it in all-valence electrons calculations [7, 20], nothing prevented taking into account the core electrons or enlarging the basis.

Coming back to our three-center index, we are led to seek an answer to the question: how many electrons are there in a three-center bond?

## 2 The three-center bond index

We restrict ourselves to the ground state of closed-shell systems, which can be described through a single-determinant wave function. The first-order density matrix is a mixed tensor [21]

$$
\begin{equation*}
2 \Pi_{a}^{b}=2 \sum_{i} x_{i a} x^{i b} \tag{1}
\end{equation*}
$$

where $x_{i a}\left(x^{i b}\right)$ are the covariant (contravariant) coefficients of the i-th occupied MO. This tensor is represented by a matrix. We may build an orbital-orbital tensor [21]

$$
\begin{equation*}
I_{b a}^{a b}=4 \Pi_{a}^{b} \Pi_{b}^{a} \tag{2}
\end{equation*}
$$

which may also be represented by a matrix; this one is symmetric (otherwise, the tensor could not be represented by a matrix), while the matrix in (1) is asymmetric for nonorthogonal bases. In these cases, there exists a convention stating that the covariant index indicates rows and the contravariant index columns of the corresponding matrix. Contracting the tensor in (2) we obtain the bond index $I_{A B}$ for the bond (formal or not) linking atoms $A$ and $B[7,21]$

$$
\begin{equation*}
I_{A B}=4 \sum_{\substack{a \in \mathcal{A} \\ b \in B}} \Pi_{a}^{b} \Pi_{b}^{a} \tag{3}
\end{equation*}
$$

This may be related with the correlation between the fluctuations of the charges $q_{A}$ and $q_{B}$ from their average values [22, 23]:

$$
\begin{equation*}
<\left(\hat{q}_{A}-<\hat{q}_{A}>\right)\left(\hat{q}_{B}-<\hat{q}_{B}>\right)>=-I_{A B} / 2 \tag{4}
\end{equation*}
$$

$\hat{q}_{A}$ being the charge operator and $[22,23]$

$$
\begin{equation*}
<\hat{q}_{A}>=q_{A}=2 \sum_{a \in A} \Pi_{a}^{a} ; N=2 \operatorname{Tr} \Pi \tag{5}
\end{equation*}
$$

The idempotency of the $\Pi$ matrix allows us to write [7, 21]

$$
\begin{equation*}
N=\left(\frac{1}{2}\right) \sum_{A, B} I_{A B} \quad ; \quad q_{A}=\left(\frac{1}{2}\right)\left(I_{A A}+\sum_{B \neq A} I_{A B}\right) \tag{6}
\end{equation*}
$$

The charge $q_{A}$ is Mulliken's gross population with a quite different partition into selfcharge and active charge [17].

Similarly [2]

$$
\begin{equation*}
N=\left(\frac{1}{4}\right) \sum_{A, B, C} I_{A B C} \quad ; \quad I_{A B C}=8 \sum_{\substack{a \in A \\ b \in B \\ c \in C}} \Pi_{a}^{b} \Pi_{b}^{c} \Pi_{c}^{a} \tag{7}
\end{equation*}
$$

Sannigrahi and Kar [3] have made an interesting observation; namely, that a higher-order bond index cannot generally be determined from a knowledge of lower-order bonds. The summation in (7) includes the possibility of equal subindices $(A, B$ or $C$ ); i.e., terms in one, two and three centers appear in $N . I_{A B C}$ is invariant for any permutation of $A, B, C$, cyclic [3] or not. This is easily seen writing the tensor equivalent to (2):

$$
\begin{equation*}
I_{a b c}^{b c a}=I_{c a b}^{a b c}=I_{a c b}^{b a c} \tag{8}
\end{equation*}
$$

For the contraction to be carried out, the order of the indices is immaterial, as long as it involves a covariant with a contravariant index; however, it cannot involve the covariant and contravariant index of the same $\Pi$ matrix, for in this case the three-center $A B C$ index splits into one-center and two-center indices.

If we write the expression for $I_{A B C}$ equivalent to eq. (4) for $I_{A B}$, we obtain [5]

$$
\begin{equation*}
<\left(\hat{q}_{A}-<\hat{q}_{A}>\right)\left(\hat{q}_{B}-<\hat{q}_{B}>\right)\left(\hat{q}_{C}-<\hat{q}_{C}>\right)>=I_{A B C} / 2 \tag{9}
\end{equation*}
$$

$I_{A B}$ uses to be positive (although it is not positive definite in non-orthogonal bases). Thus, eq. (4) means that if $q_{A}$ fluctuates in one sense from its average, value, $q_{B}$ fluctuates in the opposite sense. As to $I_{A B C}$, the three fluctuations in (9) are not likely to be all in the same sense; if two are in one sense and one in the opposite sense, either positive or negative values are to be found, with no evident connection at all with two or four electrons in the three-center bond.

If we start asking how many electrons are there in a classical bond, we have already seen that the answer is anything but clearcut. Let us briefly mention which are, to our knowledge, the most recent approaches. Covalent bond orders have been proposed [24], within the framework of Bader's topological theory of atoms in molecules [25]; they are
compared with Wiberg indices, stating (incorrectly) that both give zero for so-called noninteracting pairs of atoms [24]. On the contrary, Wiberg indices and their generalization emphasize the role of "long bonds" or "secondary bonds" [7, 21, 26, 27]; they are most important in three-center bonds [2, 3, 4, 28, 29]. A noteworthy sharing index has also been developed [8] and has been compared with covalent bond orders [30], sharing indices being half of covalent bond orders in some cases and quite close in value in most of them. We think that some of the values reported $[8,24,30]$ are too low when compared with those one could expect from chemical intuition. We find, for example, that the indices for LiH should be closer to 1 [29].

Pauling, in his obligatory reference book [31], dedicates a full chapter to one-electron and specially three-electron bonds. Even if he does not mention explicitly three-center bonds we shall see that for diborane it is possible to try a link with our formulation.

Mayer [32] has proposed a model for three-center bonds, where a single atomic orbital is assigned to each of the three centers. This model is used in Refs. [4, 33, 34]. Ref. [33] deals with $I_{A B C}$ as being a (3c-2e) index for the examples chosen. In Ref. [4], Kar states that $q_{A}+q_{B}+q_{C}=2$ for a ( $3 \mathrm{c}-2 \mathrm{e}$ ) bond. It is curious that neither of them takes into account the partition into active and self-charge.

How many electrons are there in a three-center bond, depends obviously on the model. As the self-charge is confined within the atoms, we would say that in a three-center bond $A B C$ there are $\chi$ electrons:

$$
\begin{equation*}
\chi=I_{A B}+I_{B C}+I_{A C} \tag{10}
\end{equation*}
$$

We shall see in the next section that $\chi$ is frequently neither 2 or 4 .

## 3 Results and discussion

Table 1 shows a trend in $I_{H O H}$ and $I_{H H}$, which we have found also in other $X H_{n}$-type of compounds ( $\mathrm{NH}_{3}, \mathrm{NH}_{4}^{+}$and $\mathrm{CH}_{4}$ ). Even if the fifth decimal is obviously not significant, we have reported the figures in order to evidence that $I_{X H}$ is maximum and $I_{H H^{\prime}} \cong$ $I_{H X H^{\prime}} \cong 0$ at the equilibrium position. As a consequence, due to eq. (4), the fluctuations of the $q_{H}$ 's around their average values are either zero or not correlated to each other. We have found this feature only for this type of compounds being thus, it seems, specific of the $H H^{\prime}$ correlation.

We give in Table 2 the values of $\chi$ and $I_{A B C}$ for $\mathrm{CO}_{2}$ and $C_{3}$. The Lewis description would assign four electrons each respectively in the $C=O$ and $C=C$ bonds. We have seen $[2,21]$ that these molecules have significant secondary bonds. It is quite striking that, although $\chi$ is somewhat higher than four in both of them, their three-center bond indices differ in sign.

One of the paradigms of ( $3 \mathrm{c}-2 \mathrm{e}$ ) bonds, $H_{3}^{+}$[1], has the most peculiar characteristic of being self-consistent "a priori", in the terms of Ref. [35]. That is, any quantity calculated is independent from the basis used. Thus, $\chi=1.333$ and $I_{A B C}=0.296$. Only for a model where atoms retain no charge and give up all to the bonds, the $\chi$ value can be equal to 2 .

The other usual model for a (3c-2e) bond is $B_{2} H_{6}$ [1]. Pauling [31] assigns to diborane bond numbers adding to roughly 1.5 for the BHB bond. We have $\chi=1.540$ (1.683) and $I_{B H B} 0.241$ ( 0.276 ) respectively for IEH (CNDO). In Ref. [3] $I_{B H B}$ is 0.234 (STO-3G), $0.215(4-31 \mathrm{G})$ and $0.238\left(6-31 \mathrm{G}^{*}\right)$; from the values of Ref. [36] we may get $\chi=1.370$ $(4-31 \mathrm{G})$. It is thus seen that all values of $I_{A B C}$ are in fair agreement and the available values for $\chi$ may be placed in the range 1.4-1.7 (not 2).

We have reported in Table $3 \chi$ and $I_{A B C}$ for a sample of systems. Let us examine, first of all, the paradigm for ( $3 \mathrm{c}-4 \mathrm{e}$ ) bonds, i.e. $(F H F)^{-}$. Once again, supposing that fluorine furnishes to the system only one electron, this is a ( $3 \mathrm{c}-4 \mathrm{e}$ ) bond if and only if all the charge involved is active charge. Actually, $\chi$ for all hydrogen bonds (including other ones not reported here) is approximately 1 , but $I_{A B C}$ suffers larger variations. Even if we have found that the $I_{A B C}$ values for the peptide bond NCO are of the same order of magnitude than those of strong hydrogen bonds [2], $\chi$ gives around 3 electrons for it.

For ozone we find also $\chi \simeq 3$, although the predominant resonance structures would ascribe to it six electrons [37].

For nitrous oxide $\mathrm{N}_{2} \mathrm{O}$, the values obtained for $\chi$ are consistent with the previously obtained bond indices [21] which, in turn, agree with recent studies discarding the classical hypothesis of a pentavalent nitrogen [38]. The long $N-N^{\prime}$ bond in $N_{2} O_{4}$ [39] is certainly related to the low value of $I_{N N^{\prime} O}, 5$ to 6 times less than that of $I_{O N O}$ reported in Table 3. As to $\chi$, it is $\simeq 2$ for ( $N N^{\prime} O$ ); accordingly, the very "long bond" $N O$ index is almost zero.

We have chosen to include $(\mathrm{LiH})_{2}$ in Table 4, instead of Table 3, because it decidedly has not a hydrogen bond as those of Table 3: it has a positive $I_{A B C}$ value and $\chi$ is
significantly higher. The table shows also $\chi$ and $I_{A B C}$ for $C l F_{3}$ and $S F_{4}$, where different three-center associations are possible. The values for $\chi$ split into two groups: $\chi>2$ (CNDO, STO-3G*) and a range (1.2-1.7) (IEH, STO-3G, $6-31 \mathrm{G}^{*}$ ). The CNDO approximation includes 3 d orbitals for the second-row atoms. It is therefore not surprising that CNDO performs almost as STO-3G*; it is however unexpected that the IEH values are so close to the STO-3G ones and not too different from those issuing from a $6-31 \mathrm{G}^{*}$ calculation. As to the $6-31+\mathrm{G}^{*}$ approximation, chemical intuition looses a reference frame with the introduction of diffuse functions; the very notion of an atom within a molecule becomes affected.

Inspection of the tables leads to the main conclusion that the $I_{A B C}$ 's order of magnitude and sign are fairly independent from the bases used in the calculations and that semiempirical methods are as competitive as "ab initio" ones for this kind of concepts.

In short, the number of electrons in a three-center bond is fractionary and ranges from about 1 to somewhat more than 4 .

TABLE 1 - Bond indices $I_{12}, I_{23}$ and $I_{123}$ as functions of the $H O H^{\prime}$ angle for the water molecule, number 1 labelling oxygen.

| Angle $\left(^{0}\right)$ | $I_{12}$ | $I_{23}$ | $I_{123}$ |
| :---: | :---: | :---: | :---: |
| 70 | 0.94156 | 0.03586 | 0.01078 |
| 75 | 0.95500 | 0.02386 | 0.00865 |
| 80 | 0.96461 | 0.01525 | 0.00433 |
| 85 | 0.97131 | 0.00916 | 0.00256 |
| 90 | 0.97575 | 0.00498 | 0.00138 |
| 95 | 0.97842 | 0.00227 | 0.00063 |
| 100 | 0.97965 | 0.00070 | 0.00020 |
| $\underline{105}$ | $\underline{0.97969}$ | $\underline{0.00005}$ | $\underline{0.00001}$ |
| 110 | 0.97869 | 0.00015 | 0.00004 |
| 115 | 0.97673 | 0.00091 | 0.00027 |
| 120 | 0.97385 | 0.00228 | 0.00070 |
| 125 | 0.97006 | 0.00423 | 0.00136 |
| 130 | 0.96529 | 0.00680 | 0.00227 |
| 135 | 0.95947 | 0.01002 | 0.00350 |
| 140 | 0.95255 | 0.01391 | 0.00509 |
| 145 | 0.94455 | 0.01847 | 0.00710 |
| 150 | 0.93540 | 0.02376 | 0.00960 |

TABLE $2-\chi$ and $I_{A B C}$ for $\mathrm{CO}_{2}$ and $C_{3}$, calculated following different approximations.
Geometries as in [2] and [21]. ${ }^{a}$ Ref. [3].

|  | IEH |  | CNDO |  | STO-3G |  | $4-31 \mathrm{G}^{a}$ | $6-31 \mathrm{G}^{* a}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :--- |
|  | $\chi$ | $I_{A B C}$ | $\chi$ | $I_{A B C}$ | $\chi$ | $I_{A B C}$ | $I_{A B C}$ | $I_{A B C}$ |
| $\mathrm{CO}_{2}$ | 4.459 | -0.546 | 4.134 | -0.352 | 4.326 | -0.444 |  |  |
| $C_{3}$ | 4.474 | 0.497 | 4.421 | 0.456 | 4.315 | 0.407 | 0.359 | 0.315 |

TABLE $3-\chi$ and $I_{A B C}$ for a sample of systems, calculated following different approximations. Geometries as in [2] and [21].

| System | $A B C$ | IEH |  | CNDO |  | STO-3G |  | STO-6G |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\chi$ | $I_{A B C}$ | $\chi$ | $I_{A B C}$ | $\chi$ | $I_{A B C}$ | $\chi$ | $I_{A B C}$ |
| $(\mathrm{FHF})^{-}$ | $F H F$ | 1.210 | -0.231 | 1.065 | -0.171 | 1.201 | -0.227 | 1.194 | -0.223 |
| $(\mathrm{HOHOH})^{-}$ | OHO | 1.240 | -0.248 | 1.079 | -0.175 | 1.117 | -0.191 | 1.112 | -0.189 |
| $(\mathrm{FH})_{2}$ | FHF | 1.037 | -0.096 | 0.946 | -0.005 | 0.961 | -0.013 | 0.954 | -0.011 |
| $\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$ | OHO | 1.014 | -0.052 | 0.981 | -0.005 | 0.963 | -0.015 | 0.954 | -0.014 |
| Formamide | NCO | 3.143 | -0.224 | 3.136 | -0.161 | 3.151 | -0.184 | 3.146 | -0.183 |
| $\mathrm{Gly.Gly}$ | NCO | 3.081 | -0.208 | 3.022 | -0.155 | 3.090 | -0.170 | 3.087 | -0.170 |
| $\mathrm{O}_{3}$ | OOO | 3.235 | -0.278 | 3.130 | -0.286 | 2.831 | -0.346 | 3.205 | -0.326 |
| $\mathrm{~N}_{2} \mathrm{O}$ | NNO | 4.521 | -0.532 | 4.232 | -0.344 | 4.197 | -0.455 | 4.194 | -0.454 |
| $\mathrm{~N}_{2} \mathrm{O}_{4}$ | ONO | 3.382 | -0.292 | 3.319 | -0.268 | 3.524 | -0.358 | 3.523 | -0.358 |

TABLE $4-\chi$ and $I_{A B C}$ for $(L i H)_{2}, C l F_{3}$ and $S F_{4}$, calculated following different approximations. The geometry of $(\mathrm{LiH})_{2}$ is taken from Ref. [40], that of $\mathrm{ClF}_{3}$ from Ref. [42] and that of $S F_{4}$ from Ref. [43]. ${ }^{a}$ Ref. [3]. ${ }^{b}$ Ref. [41]. ${ }^{c}$ Ref. [4].

|  | IEH |  | CNDO |  | STO-3G |  | 6-31G* |  | STO-3G* |  | 6-31+G* |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\chi$ | $I_{A B C}$ | $\chi$ | $I_{A B C}$ | $\chi$ | $I_{A B C}{ }^{c}$ | $\chi$ | $I_{A B C}{ }^{\text {c }}$ | $\chi$ | $I_{A B C}{ }^{\text {c }}$ | $\chi$ | $I_{A B C}{ }^{c}$ |
| $\begin{gathered} (\mathrm{LiH})_{2} / A B C \\ L i H L i \end{gathered}$ | 1.292 | 0.195 | 1.493 | 0.245 |  | $0.241^{a}$ | $1.23{ }^{\text {b }}$ | $0.177^{a}$ |  |  |  |  |
| $\begin{gathered} C l F_{3} / A B C \\ F_{a} C l F_{a} \end{gathered}$ | 1.408 | -0.116 | 2.153 | -0.027 | 1.406 | -0.163 | 1.254 | -0.080 | 2.145 | -0.049 -0.054 | 0.9990 1.340 | $-0.068$ <br> -0.039 |
| $\mathrm{F}_{a} \mathrm{ClF} \mathrm{F}_{e}$ | 1.453 | -0.139 | 2.256 | -0.019 | 1.465 | -0.124 | 1.457 | -0.037 | 2.201 | -0.054 | 1.340 | -0.039 |
| $\begin{aligned} & \hline S F_{4} / A B C \\ & F_{a} S F_{a} \end{aligned}$ | 1.467 | -0.133 | 2.236 | -0.016 | 1.422 | -0.116 | 1.371 | -0.027 | 2.227 | -0.020 | 0.870 | 0.018 |
| $F_{a} S F_{a}$ $F_{e} S F_{e}$ | 1.672 | -0.044 | 2.499 | -0.023 | 1.684 | -0.049 | 1.739 | -0.026 | 2.435 | -0.040 | 1.577 | -0.034 |
| $F_{a} S F_{e}$ | 1.580 | -0.093 | 2.373 | -0.029 | 1.561 | -0.083 | 1.553 | -0.029 | 2.348 | -0.050 | 1.195 | 0.023 |

## REFERENCES

[1] R.L. DeKock and W.B. Bosma, J. Chem. Educ. 65 (1988) 194.
[2] M. Giambiagi, M.S. de Giambiagi and K.C. Mundim, Struct. Chem. 1 (1990) 423.
[3] A.B. Sannigrahi and T. Kar, Chem. Phys. Lett. 173 (1990) 569.
[4] T. Kar and E.S. Marcos, Chem. Phys. Lett. 192 (1992) 14.
[5] K.C. Mundim, M. Giambiagi and M.S. de Giambiagi, CBPF-NF-048/93; to be published.
[6] C.A. Coulson, Proc. Roy. Soc. London A169 (1939) 143.
[7] M. Giambiagi, M.S. de Giambiagi, D.R. Grempel and C.D. Heymann, J. Chim. Phys. 72 (1975) 15.
[8] R.L. Fulton, J. Phys. Chem. 97 (1993) 7516.
[9] K. Ruedenberg, J. Chem. Phys. 22 (1954) 1878.
[10] G.V. Bykov, Electronic charges of bonds in organic compounds (Pergamon Press, N. York, 1964), chap. 1.
[11] A. Julg and P. Julg, Int. J. Quantum Chem. 13 (1978) 483.
[12] A. Julg, Int. J. Quantum Chem. 27 (1984) 709.
[13] R.S. Mulliken, J. Chem. Phys. 23 (1955) 1833.
[14] R. Hoffmann, J. Chem. Phys. 39 (1963) 1397; — 40 (1964) 2474.
[15] J.A. Pople and D.L. Beveridge, Approximate molecular orbital theory (McGraw-Hill, N. York, 1970).
[16] K. Wiberg, Tetrahedron 24 (1968) 1083.
[17] C. Trindle, J. Am. Chem. Soc. 91 (1969) 219.
[18] R. Bingham, M.J.S. Dewar and D.H. Lo, J. Am. Chem. Soc. 97 (1975) 1285, 1294, 1302, 1307, 1311.
[19] M.J.S. Dewar and W. Thiel, J. Am. Chem. Soc. 99 (1977) 4899.
[20] M. Giambiagi, M.S. de Giambiagi and W.B. Filho, Chem. Phys. Lett. 78 (1981) 541.
[21] M.S. de Giambiagi, M. Giambiagi and F.E. Jorge, Z. Naturforsch. 39a (1984) 1259.
[22] M.S. de Giambiagi, M. Giambiagi and F.E. Jorge, Theor. Chim. Acta 68 (1985) 337.
[23] K.C. Mundim, J. Phys. France 50 (1989) 11.
[24] J. Cioslowski and S.T. Mixon, J. Am. Chem. Soc. 113 (1991) 4142.
[25] R.F.W. Bader, Y. Tal, S.G. Anderson and T.T. Nguyen-Dang, Isr. J. Chem. 19 (1980)8; R.F.W. Bader, T.T. Nguyen-Dang and Y. Tal, Rep. Prog. Phys. 44 (1981) 893; R.F.W. Bader and T.T. Nguyen-Dang, Adv. Quantum Chem. 14 (1981) 63.
[26] M. Giambiagi, M.S. de Giambiagi and K.C. Mundim, J. Chem. Soc. Faraday Trans. 88 (1992) 2995.
[27] R.D. Harcourt, J. Mol. Structure 300 (1993) — and Refs. therein.
[28] A.B. Sannigrahi and T. Kar, Chem. Phys. Lett. 173 (1990) 569.
[29] A.B. Sannigrahi, Adv. Quantum Chem. 23 (1992) 301.
[30] R.L. Fulton and S.T. Mixon, J. Phys. Chem. 97 (1993) 7530.
[31] L. Pauling, The nature of the chemical bond (Cornell University Press, Ithaca, N. York, 1960 , chap. 10 , particularly 10.7).
[32] I. Mayer, J. Mol. Structure (Theochem) 186 (1989) 43.
[33] T. Kar and K. Jug, J. Mol. Structure (Theochem) 283 (1993) 177.
[34] T. Kar, J. Mol. Structure (Theochem) 283 (1993) 313.
[35] P.K. Mehrotra and R. Hoffmann, Theor. Chim. Acta 48 (1978) 301.
[36] A.B. Sannigrahi, P.K. Nandi, L. Behera and T. Kar, J. Mol. Structure (Theochem) 276 (1992) 259.
[37] F.A. Cotton and G. Wilkinson, Advanced Inorganic Chemistry (Interscience, N. York, 1966, p. 365)
[38] M.N. Glukhotsev and P. von R. Schleyer, Chem. Phys. Lett. 198 (1992) 547.
[39] R. Harcourt, Croat. Chem. Acta 64 (1991) 399 and earlier Refs. therein.
[40] H. Kato, K. Hirao and K. Akagi, Inorg. Chem. 20 (1981) 3659.
[41] A.B. Sannigrahi and T. Kar, J. Mol. Structure (Theochem) 180 (1988) 149.
[42] L.M. Petterson, P.E.M. Siegbahn and O. Gropen, Mol. Phys. 48 (1983) 871.
[43] W.M. Tolles and W.D. Gwin, J. Chem. Phys. 36 (1962) 1119.

